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Francesco Aieta
Ali Kabiri
Patrice Genevet
Nanfang Yu
Mikhail A. Kats
Zeno Gaburro
Federico Capasso

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Francesco Aieta, ${ }^{\text {a,b }}$ Ali Kabiri, ${ }^{\text {a }}$ Patrice Genevet, ${ }^{\text {a,c }}$ Nanfang Yu, ${ }^{\text {a }}$ Mikhail A. Kats, ${ }^{\text {a }}$ Zeno Gaburro, ${ }^{\text {a,d }}$ and Federico Capasso ${ }^{\text {a }}$<br>${ }^{a}$ Harvard University, School of Engineering and Applied Sciences, Cambridge, Massachusetts 02138<br>capasso@seas.harvard.edu<br>${ }^{\text {b }}$ Università Politecnica delle Marche, Dipartimento di Scienze e Ingegneria della Materia, dell'Ambiente ed Urbanistica, via Brecce Bianche, 60131 Ancona, Italy<br>${ }^{\text {c }}$ Texas A\&M University, Institute for Quantum Studies and Department of Physics, College Station, Texas, 77843<br>${ }^{\mathrm{d}}$ Università degli Studi di Trento, Dipartimento di Fisica, via Sommarive 14, 38100 Trento, Italy


#### Abstract

A three-dimensional extension of the recently demonstrated generalization of the laws of refraction and reflection was investigated for both flat and curved metasurfaces. We found that out-of-plane refraction occurs for a metasurface that imparts a wavevector out of the plane of incidence onto the incident light beam. Metasurfaces provide arbitrary control over the direction of refraction, and yield new critical angles for both reflection and refraction. A spherical metasurface with phase discontinuities leads to unconventional light bending compared to standard refractive lenses. © 2012 Society of Photo-Optical Instrumentation Engineers (SPIE). [DOI: 10.1117/1 .JNP.6.063532]


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## 1 Introduction

The formulation of laws of reflection and refraction dates to the 10th century when Alhazen conducted experiments on the movement of light passing through different media, ${ }^{1}$ and Ibn Sahl deduced the law of refraction. ${ }^{2}$ These laws have been reported in a simple mathematical formulation in the works of Thomas Herriot, Willebrord Snell, and Rene Descartes. ${ }^{3}$ Eventually, Pierre de Fermat generalized these laws to determine the path of a ray of light traveling in media with an arbitrary distribution of refractive indices. ${ }^{4}$ Recently, recalling a concept previously introduced by Veselago, ${ }^{5}$ Pendry suggested using negative refractive index materials to modify the refraction of light. ${ }^{6}$ Some years later, the concept of transformation optics was introduced, ${ }^{7}$ which is a method to control light propagation based on a complicated distribution of the optical refractive index of a heterogeneous material or metamaterial. These concepts led to the experimental demonstration of intriguing effects, such as negative refraction, subwavelengthfocusing, and optical cloaking. ${ }^{8-10}$ However, in all of these demonstrations the redirecting of a light beam is a result of gradual phase accumulation along the beam path through the material or metamaterial.

Recently Snell's law has been revisited and generalized by using metasurfaces that introduce abrupt phase shifts along the optical path. ${ }^{11}$ The bending of the refracted beam is not only determined by the refractive index jump at the interface but also by a distribution of phase discontinuities imposed by a metasurface comprising an array of ultrathin and subwavelength-spaced optical antennas. This leads to anomalous reflection and refraction of light ${ }^{11,12}$ that can be even directed out of the plane the incidence. This effect has been experimentally observed for the

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Fig. 1 The principle of stationary phase is used to derive the trajectory of a beam of light refracted from an interface separating two media. We consider two infinitesimally close paths from the point $P_{i}$, located in the medium with refractive index $n_{i}$, and $P_{t}$, located in the medium with refractive index $n_{t}$. The difference of the phases accumulated along the paths $P_{i} A P_{t}$ and $P_{i} B P_{t}$ has to be zero, where $A$ and $B$ are points arbitrarily selected on the interface and infinitesimally close to each other. The phase difference should include a contribution due to the arbitrarily oriented phase gradient on the interface.
reflection and refraction of an optical beam from a flat surface with a component of the phase gradient pointing out of the plane of incidence. ${ }^{13}$ The concept of phase discontinuities has also been applied to demonstrate other effects, such as the generation of vortex beams ${ }^{14}$ and focusing free from on-axis aberration. ${ }^{15}$ In this letter, we study refraction and reflection in a more general geometry, in which a constant gradient of phase discontinuities is imposed on curved interfaces. In particular, we derive the generalized Snell's law for flat and spherical interfaces.

In its original formulation, Fermat's principle states that the trajectory taken between two points, $P_{i}$ and $P_{t}$, by a ray of light is that of the least optical path, i.e., the physical length multiplied by the refractive index. ${ }^{4}$ A more general form of the principle, known as the principle of stationary phase, states that the derivative of the phase accumulated along the actual light path, is zero with respect to infinitesimal variations of the path. ${ }^{4}$

Now, let us consider a ray of light with wave vector $k_{i}$ incident on a curved interface that introduces a constant phase gradient $\nabla \Phi$ oriented along an arbitrary direction along the interface, and separates two media of indices $n_{i}$ and $n_{t}$, respectively. The direction of the refracted ray with wave vector $k_{t}$ can be derived using the principle of stationary phase; the difference of phase accumulated by light travelling along two different paths infinitesimally close to each other has to be zero (Fig. 1):

$$
\begin{equation*}
\delta \int \varphi \mathrm{d} r=\delta\left[\int k_{i} \cdot \mathrm{~d} r+\nabla \Phi \cdot s+\int k_{t} \cdot \mathrm{~d} r\right]=\left(k_{i}-k_{t}+\nabla \Phi\right) \cdot \mathrm{d} s=0 \tag{1}
\end{equation*}
$$

where $r$ and $s$ are the position vector in space and its projection on the interface, respectively. Equation (1) is valid for all $\mathrm{d} s$ on the interface; therefore, the vector $\left(k_{i}-k_{t}+\nabla \Phi\right)$ should be perpendicular to the tangent to the surface at the point of incidence. Hence we have,

$$
\begin{equation*}
\hat{n} \times\left(k_{t}-k_{i}\right)=\hat{n} \times \nabla \Phi \tag{2}
\end{equation*}
$$

Accordingly, a similar relation can be derived for the reflected beam of light:

$$
\begin{equation*}
\hat{n} \times\left(k_{r}-k_{i}\right)=\hat{n} \times \nabla \Phi . \tag{3}
\end{equation*}
$$

To illustrate the generality of the proposed relations, the reflection and refraction of a light beam are studied at flat and spherical interfaces.

## 2 Flat Interface

Figure 2 shows reflection and refraction of a ray of light impinging on a flat surface with an angle $\vartheta_{i}$ with respect to the $z$-axis. Without loss of generality, the plane of incidence is the $y z$-plane and the interface is along the $x y$-plane. Therefore the unit vector $\hat{n}=\hat{z}$ and the incident vector $k_{i}$ has two non-zero components such that $k_{i}=\left(0, k_{y, i}, k_{z, i}\right)$. The flat plane imparts an abrupt phase


Fig. 2 Reflection and refraction from a flat interface with a constant gradient of phase discontinuities. A beam is incident onto the interface separating two media with refractive indices $n_{i}$ and $n_{t}$, respectively, forming an angle $\vartheta_{i}$ with respect to the $z$-axis. The plane of incidence is the $y z$-plane. We describe the directions of the off-plane refracted and reflected beams with angles $\vartheta_{t(r)}$ (the angle between the refracted (reflected) beam and its projection on the $x z$-plane) and $\varphi_{r(t)}$ (the angle formed by the projection of refracted (reflected) beam on the $x z$-plane and the $z$-axis).
jump to the incident wave, characterized by a constant gradient $\nabla \Phi$ oriented along an arbitrary direction with respect to the plane of incidence.

We can work out Eq. (2) for this geometry, obtaining: ${ }^{13}$

$$
\left\{\begin{array}{c}
k_{x, t}=\frac{\mathrm{d} \Phi}{\mathrm{~d} x}  \tag{4}\\
k_{y, t}=k_{y, i}+\frac{\mathrm{d} \Phi}{\mathrm{~d} y}
\end{array}\right.
$$

Due to the lack of translational invariance along the interface, the tangential wavevector of light is not conserved; the interface contributes additional terms $\mathrm{d} \Phi / \mathrm{d} x$ and $\mathrm{d} \Phi / \mathrm{d} y$, which allow one to control the refracted beam along both $x$ and $y$ directions. Hence, the refracted ray of light does not necessarily lie in the plane of incidence.

We use angles $\vartheta_{i}$ and $\varphi_{t}$ to describe the direction of the refracted beam (see Fig. 2) and obtain the following generalized law of refraction in three-dimensions: ${ }^{13}$

$$
\left\{\begin{array}{l}
\cos \vartheta_{t} \sin \varphi_{t}=\frac{1}{n_{t} k_{0}} \frac{\mathrm{~d} \Phi}{\mathrm{~d} x}  \tag{5}\\
n_{t} \sin \vartheta_{t}-n_{i} \sin \vartheta_{i}=\frac{1}{k_{0}} \frac{\mathrm{~d} \Phi}{\mathrm{~d} y}
\end{array}\right.
$$

Similarly, using Eq. (3) we obtain the generalized law of reflection in three dimensions (Fig. 2).

$$
\left\{\begin{array}{l}
\cos \vartheta_{r} \sin \varphi_{r}=\frac{1}{n_{i} k_{0}} \frac{\mathrm{~d} \Phi}{\mathrm{~d} x}  \tag{6}\\
\sin \vartheta_{r}-\sin \vartheta_{r}=\frac{1}{n_{i} k_{0}} \frac{\mathrm{~d} \Phi}{\mathrm{~d} y}
\end{array}\right.
$$

Note that when the phase gradient is oriented along the plane of incidence $\left(\frac{\mathrm{d} \Phi}{\mathrm{d} x}=0\right)$ the reflected and refracted beams are also in this plane, and if both components of the phase gradient are zero, the conventional law of refraction is restored.

In conventional refraction, the critical angle is the angle above which total internal reflection occurs. An interface with a phase gradient arbitrarily oriented with respect to the plane of incidence alters the relations between the tangential components of the incident, reflected and refracted $k$-vector and consequently gives rise to new critical angles for both reflection and refraction. The new critical angles are reached when the refracted or reflected beams become evanescent, which means that the respective wave vectors are imaginary in the propagation direction. This condition is found by equating the tangential component of $k_{t(r)}$ to the modulus of the $k$-vector in the hosting medium:

$$
\begin{equation*}
k_{\| \mid, t(r)}=\sqrt{k_{x, t(r)}^{2}+k_{y, t(r)}^{2}}=n_{t(i)} k_{0} . \tag{7}
\end{equation*}
$$

From Eqs. (4), (5), and (7) we can derive the following expressions for the critical angles for transmission:

$$
\begin{equation*}
\vartheta_{i}^{c, t}=\sin ^{-1}\left[ \pm \frac{1}{n_{i}} \sqrt{n_{t}^{2}-\left(\frac{1}{k_{0}} \frac{\mathrm{~d} \Phi}{\mathrm{~d} x}\right)^{2}}-\frac{1}{n_{i} k_{0}} \frac{\mathrm{~d} \Phi}{\mathrm{~d} y}\right] \tag{8}
\end{equation*}
$$

As already mentioned, the presence of the phase gradient breaks the translational invariance, and therefore the critical angles are not symmetric with respect to the $x z$-plane.

Equation (6) exhibits a nonlinear relationship between the angle of reflection and the incident angle, which yields two critical angles for reflection:

$$
\begin{equation*}
\vartheta_{i}^{c, r}=\sin ^{-1}\left[ \pm \sqrt{1-\left(\frac{1}{n_{i} k_{0}} \frac{\mathrm{~d} \Phi}{\mathrm{~d} x}\right)^{2}}-\frac{1}{n_{i} k_{0}} \frac{\mathrm{~d} \Phi}{\mathrm{~d} y}\right] . \tag{9}
\end{equation*}
$$

Figure 3 shows the critical angles versus the normalized gradients $\frac{\mathrm{d} \Phi}{\mathrm{d} x} / \frac{2 \pi}{\lambda_{0}}$ and $\frac{\mathrm{d} \Phi}{\mathrm{d} y} / \frac{2 \pi}{\lambda_{0}}$. The gray shaded areas are regions at which transmission/reflection exist for all incident angles. Unlike conventional refraction and reflection, we can design interfaces with no critical angles, or interfaces featuring critical angles only in reflection while preserving the transmission for all incident angles and vice versa (see Fig. 3).

A demonstration of the generalized refraction law in three dimensions, and out-of-plane refraction from a flat interface, is presented using an interface patterned with an array of optical antennas. ${ }^{13}$ By suitably designing their geometry one can control the phase and amplitude of


Fig. 3 The map shows the critical angles of transmission and reflection calculated for a light beam traveling from silicon $\left(n_{i}=3.41\right)$ to air $\left(n_{t}=1\right)$ through an interface with a gradient of phase discontinuities. The varying values of phase gradient along the in-plane ( $y$ axis) and out-of-plane ( $x$ axis) directions are normalized by the factor $\frac{2 \pi}{\lambda_{0}}$. (a) and (b) are the positive and the negative critical angles for transmission; (c) and (d) for reflection. The gray-shaded areas are the regions for which transmission and reflection exist for all of the incident angles. The black square indicates a phase gradient value for which critical angle of reflection exists while refraction is preserved for all incident angles [gray area in (a) and (b)]. For the phase gradient corresponding to the blue (red) circle the critical angle for transmission is at 35 deg. ( -35 deg.) while the reflected beam is preserved for all the incident angles.


Fig. 4 (a) Sketch of the experimental setup. The incident light generated by a quantum cascade laser $(\lambda=8 \mu \mathrm{~m})$ impinges on the interface at an angle $\vartheta_{i}$ with respect to the $z$-axis. The interface ( $x y$-plane at $z=0$ ) is between silicon ( Si , refractive index $n_{i}=3.41$ ) and air ( $n_{1} t=1$ and light is incident from the Si side. We call $\vartheta_{t}^{o}$ the conventional refraction angle, while $\vartheta_{t}^{a}$ and $\varphi_{t}^{a}$ characterize the anomalous refraction. (b) Angles of refraction as a function of angle of incidence and phase gradient orientation $\alpha$. The black line is the theoretical curve from the classical Snell's law. Colored lines are theoretical curves calculated from Eq. (5) for different phase gradient orientations. Circles correspond to the measured angles ( $\vartheta_{t}^{o}$ black circles, $\vartheta_{t}^{a}$ and $\varphi_{t}^{a}$ colored circles).
light scattered by each antenna to generate the desired wavefront. ${ }^{16,17}$ The sample is created by periodically translating in the $x-y$ plane the unit cell consisting of 8 subwavelength $V$-shaped antennas [colored in yellow in the inset scanning electron microscope image of Fig. 4(a)]. The array imposes a phase gradient on the interface in the direction $s$ that forms an angle $\alpha$ with the $y$-axis as shown in the inset. When $\alpha$ is not zero, a component of the phase gradient points out of the plane of incidence, resulting in an out-of-the-plane scattered beam. The antennas were designed such that they need to be excited with a linear polarization at an angle of 45 deg, with respect to the antenna symmetry axes. ${ }^{11,16}$ To maintain this configuration when the sample is rotated, we simultaneously rotated the incident polarization.

As described in Ref. 11 part of the light is reflected and refracted according to the conventional laws in the same polarization as the incident beam. Anomalously reflected and refracted beams are also generated, as described by Eqs. (5) and (6), which are cross-polarized with respect to the incident beam.

To validate the predictions of the 3-D law of refraction [Eq. (5)], we performed an experimental study of anomalous refraction for various incidence angles $\vartheta_{i}$ and phase gradient orientations ( $\alpha$ angles). The magnitude of the phase gradient is fixed to $|\nabla \Phi|=2 \pi / 15 \mu \mathrm{~m}$ for all the experiments. The results are summarized in Fig. 4(b), which unambiguously show out-of-plane refraction with $\varphi_{t} \neq 0$. Additionally, the phase gradient orientation changes the out-of-plane refraction angles in good agreement with Eq. (5). It is worth noting that regardless of the different orientations of the phase gradient, the ordinarily refracted beam always lies in the plane of incidence, at angles predicted by the conventional Snell's law. Our experimental setup did not allow us to monitor the reflected beam.

## 3 Spherical Interface

Figure 5 shows the schematic of refraction of a light beam at a spherical interface with radius $R$, which introduces a constant gradient of phase shift $\nabla \Phi$ to the incident light. The incident beam lies in the $y z$-plane and the interface is at $\rho=R$ in the spherical reference system. Therefore we have $\hat{n}=-\hat{\rho}$ and $\left(k_{\rho, i}, k_{\theta, i}, 0\right)$.


Fig. 5 (a) Refraction from a spherical interface with radius $R$ and a constant phase gradient $\nabla \Phi$ along the surface. The incident beam comes from the medium with index $n_{i}$ in the $y z$-plane and gets refracted in the medium with index $n_{t}$. A spherical coordinate system is used. (b) Twodimensional sketch of a simplified geometry where the incident and refracted beams lie on the $y z$-plane.

From Eq. (2) we obtain:

$$
\left\{\begin{array}{l}
k_{\phi, t}=\frac{\mathrm{d} \Phi}{\mathrm{~d} \phi}  \tag{10}\\
k_{\theta, t}=k_{\theta, i}+\frac{\mathrm{d} \Phi}{\mathrm{~d} \theta}
\end{array}\right.
$$

By imposing these equalities for the component of the $k$-vector tangential to the interface, one can easily obtain the direction of the refracted beam, which in general does not lie in the plane of incidence. Similar equations can be obtained for reflection.

To see the effect of a constant phase gradient on a spherical interface, we consider a pencil of rays parallel to the $z$-axis and assume $n_{i}>n_{t}$. We simplify the geometry by taking a cross section along the $y z$-plane, as shown in Fig. 5(b). In the absence of a phase gradient the rays will be refracted towards a point located on the $z$-axis at a distance from the interface that depends on the ratio of the refractive indices of the two media. The refraction from a spherical interface is commonly used in lenses and it can be easily shown that in the limit of the paraxial approximation, all the rays will converge to the focal point. ${ }^{3}$ Given this approximation, the distance $f$ at which a ray will intersect the $z$-axis is: $f=R \frac{\vartheta_{1}}{\vartheta_{t}-\theta_{i}}$. Using the approximately linear relation between the angle of incidence and the angle of refraction $\left(n_{t} \vartheta_{t} \cong n_{i} \vartheta_{i}\right)$ we can obtain $f=R \frac{n_{i}}{n_{t}-n_{i}}$, which is the common expression derivable from the Lensmaker's Formula ${ }^{4}$ for a plano-convex lens.

If now we consider an interface with a gradient of phase discontinuities, from Eq. (10) we can derive a relation between the angle of incidence and the angle of refraction. Assuming paraxial approximation and small phase gradient pointing in the $\hat{\theta}$ direction $\nabla \Phi=\frac{\mathrm{d} \Phi}{\mathrm{d} \theta} \hat{\theta}$, we obtain:

$$
\begin{equation*}
n_{t} \vartheta_{t}=n_{i} \vartheta_{i}+\frac{1}{k_{0}} \frac{\mathrm{~d} \Phi}{\mathrm{~d} \theta} \tag{11}
\end{equation*}
$$

By substituting Eq. (11) in the expression of $f=R \frac{\vartheta_{1}}{\vartheta_{t}-\vartheta_{i}}$, one can see that the latter is still a function of the incident angle. This means that a spherical interface with a phase gradient does not refract a paraxial beam to a single point and therefore cannot be used to focus light.

## 4 Concluding Remarks

We derived generalized laws of reflection and refraction for interfaces with phase discontinuities. These laws are general and can be adapted to various geometries. To illustrate the generality of the generalized laws, the reflection and refraction of a light beam are studied at both flat and spherical interfaces.

From the conservation of the tangential component of the $k$-vector, which originates from Fermat's principle, we derived the expressions for the angles describing the out-of-plane
reflection and refraction. New critical angles follow from these nonlinear expressions for both reflected and refracted beams.

Finally, we showed that a spherical interface separating two media does not focus light to a single point in the presence of a constant phase gradient, even in the limit of paraxial approximation. Nonetheless, a flat interface with phase gradient can be used to focus light if a nonlinear phase distribution is used. This design has been recently demonstrated, ${ }^{15}$ showing the capability of light focusing without spherical aberrations.

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Francesco Aieta received his BS and MS degrees with honors in electrical engineering from the Università Politecnica delle Marche, Ancona, in 2007 and 2009, respectively. He is working toward a PhD at the Dipartimento di Scienze e Ingegneria della Materia, dell'Ambiente ed Urbanistica at the same university. Since January 2011, he has been enrolled in a research fellowship program at the School of Engineering and Applied Sciences at Harvard University, Cambridge, Massachusetts. His current activity focuses on plasmonic metainterfaces and nanoscale metallic optical antennas. Other areas of interest include optical trapping and properties of liquid crystals. He is a member of the Optical Society of America.


Ali Kabiri is currently a postdoctoral research-fellow at Harvard University, focusing on metasurfaces and their applications at optical frequencies and magneto-surface plasmon resonances. He received his BE degree in electrical engineering from Sharif University of Technology, Iran, and MS degree in theoretical physics in 2002. He pursued a career in industry at a digital-display manufacturing plant, and served as a sectional manager for Samsung IT-product service center in Iran. He received his PhD degree in electromagnetics/RF design from Waterloo University, Canada (2010), followed by a researcher position at Quebec University. In 2012, he received the Canadian National Science and Engineering Research Council postdoctoralfellowship.


Patrice Genevet received his PhD degree in physics from the university of Nice-Sophia-antipolis, France, 2009. During his PhD, he demonstrated that two coupled micro-resonators can operate as a cavity soliton laser. In 2009, he joined Capasso's group at Harvard University in collaboration with M.O. Scully in Texas A\&M University to work on nonlinear plasmonics and metasurfaces. Since 2011, he is research associate at Harvard University with Capasso. His research interests include semiconductor lasers, nanophotonics, plasmonics, metamaterials, metasurfaces, nonlinear optics, and nonlinear dynamics.


Nanfang Yu received his BS degree in electronic information science and technology from the Department of Electronics, Peking University, Beijing, China, in 2004, and a PhD degree in engineering sciences from Harvard University, Cambridge, Massachusetts, in June 2009. Currently, he is a research associate in the School of Engineering and Applied Sciences at Harvard. He has worked extensively on plasmonics, metamaterials, and mid-infrared and terahertz semiconductor lasers. He will be an assistant professor of applied physics at the Department of Applied Physics and Applied Mathematics, Columbia University, starting in January 2013.

He is a member of the Optical Society of America, the American Physical Society, and the Materials Research Society.


Mikhail A. Kats received his BS in engineering physics from Cornell University (Ithaca, New York) in 2008, and his SM in applied physics from Harvard University (Cambridge, Massachusetts) in 2010. He is currently working toward his PhD in applied physics at Harvard University, specializing in nano-optics and plasmonics, and is supported by a National Science Foundation Graduate Research Fellowship. He has previously carried out research at Cornell University and the Palo Alto Research Center. To date, he has authored and co-authored 18 articles in peer-reviewed journals.


Zeno Gaburro received the Italian graduation summa cum laude in electrical engineering from Politecnico di Milano (Italy) in 1992, and his PhD in electrical engineering from University of Illinois at Chicago in 1998. He was under a fellowship at Argonne National Laboratory (Argonne, Illinois, 1997), was a process characterization engineer at AMS International a.G. (Austria, 1998 to 1999), and has been at the University of Trento (Italy) since 1999, where he presently holds a position as senior researcher. He has served on a Review Board for the Finnish Ministry of Education, held a symposium chair at SPIE annual meetings from 2002 to 2007, and has been Visiting Scholar in the Capasso Group at SEAS, Harvard University, since late 2008, supported by the FP7 Marie Curie by European Union. His current main interests include plasmonics, optical antennas, and metamaterials. He is a member of OSA and SPIE.


Federico Capasso received his PhD degree (summa cum laude) from the University of Rome, Italy, in 1973. From 1974 to 1976, he was a researcher at Fondazione UgoBordoni. In 1976, he joined Bell Laboratories, where he was a member of the technical staff (1977 to 1986), department head (1986 to 2000), vice president for physical research (2000 to 2002), and was made a Bell Laboratories Fellow for his scientific contributions in 1997. He is currently the Robert Wallace professor of Applied Physics and Vinton Hayes senior research fellow in electrical engineering at Harvard University, Cambridge, Massachusetts. He has been engaged in basic and applied research on the quantum design of new artificial materials and devices, known as band structure engineering, and also in investigations of the Casimir effect, and the field of surface plasmon photonics. He is a co-inventor of the quantum cascade laser.


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